ملتقى مهارات المعلمين Teacher Skills Forum

Using Computer Algebra Systems to Build Stronger Understanding

Nevil Hopley

From What to How

Using Computer Algebra Systems (CAS) to Build Stronger Understanding



Nevil Hopley

T³ National Trainer, Scotland & UK.

Head of Mathematics Department, George Watson's College, Edinburgh

www.calculatorsoftware.co.uk/nspire

This talk will have a....

A Beginning

Background information about me & CAS, and the remit of this talk.

A Middle

CAS activities covering various different maths topics for students aged 12-18 years.

An End

...in 40 minutes' time!

And you can download all that you see today from

www.calculatorsoftware.co.uk/nspire

Curious Questions



CAS ... what it's not!

Google

cas	Ŷ	Q
cash converters cash generator casio casualty		

Press Enter to search.

Citizens Advice Scotland **C**entral **A**llocation **S**ystem **C**ESG **A**ssured **S**ervice **C**ensus **A**rea **S**tatistics Chief of Air Staff Cinema Audio Society Computing At School Contained Air Solutions Centre of African Studies **C**onsulting **A**rborist **S**ociety Chemical Abstracts Service **C**onfirmation of **A**cceptance for **S**tudies **C**loud **A**pplications and **S**ecurity Centre for American Studies **C**ourt of **A**rbitration for **S**port Churches Agency for Safeguarding **C**ommunications **A**dvisory **S**ervice Centre for Atmospheric Science Circuits And Systems Research Group **C**ommunity **A**ction **S**outhwark



Texas Instruments Nspire CX-CAS Graphic Calculator with ... www.amazon.co.uk > ... > Office Electronics > Calculators > Graphing ~ Texas Instruments Nspire CX-CAS Graphic Calculator with Touchpad: Amazon.co.uk: Office Products.

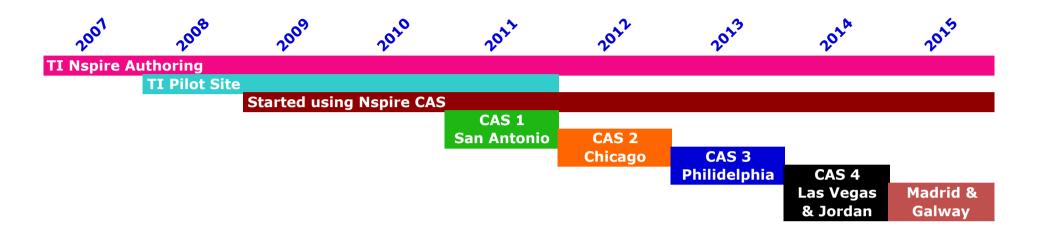


CAS View - GeoGebraWiki

wiki.geogebra.org/en/CAS_View *

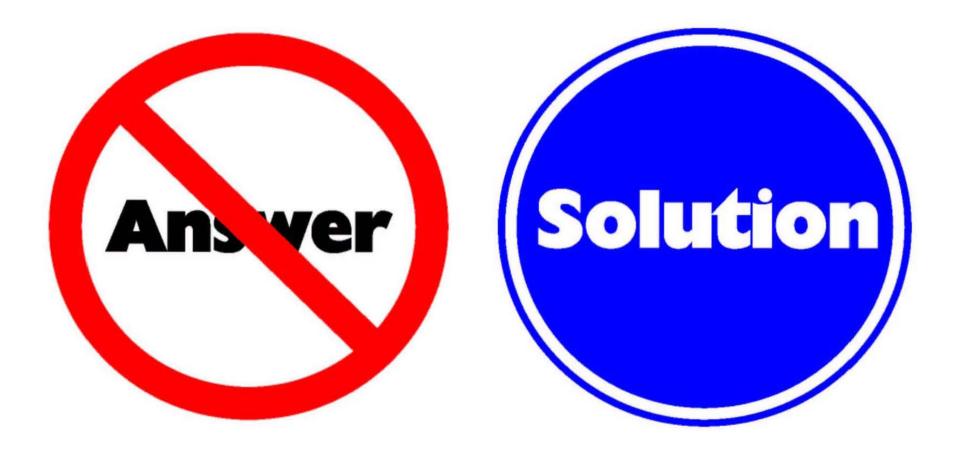
The CAS View allows you to use GeoGebra's CAS (Computer Algebra System) for symbolic computations. It consists of cells with an Input Field at the top and ...

My CAS Timeline

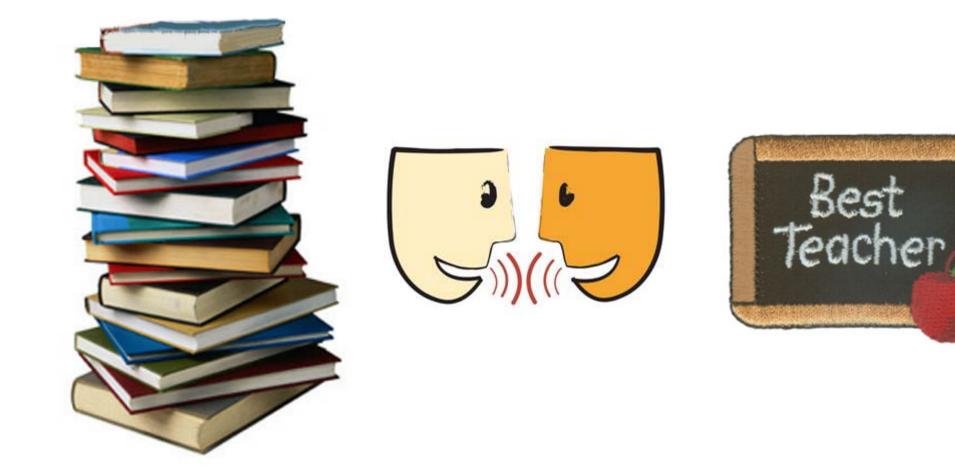


CAS Talks at TI International & European Conferences

- 2011 My first 18 months of CAS usage
- 2012 Trigonometry and Rearranging Equations
- 2013 Linear Equations and Units
- 2014 Extending CAS with functions and programs
- 2015 CAS in Statistics



Not Allowed in Exams



Allowed in Exams



Scottish Exam Arrangements Documents

"Calculators with mathematical and graphical facilities and those with computer algebra systems (CAS) can be utilised as powerful tools both for processing data, especially in the study of statistics, and for reinforcing mathematical concepts."

"The elementary calculus studied ... is extended to differentiation of sums, products, quotients and composites of elementary functions and to integration using standard results and substitution methods respectively. ...Computer algebra systems can be used extensively for consolidation and extension."

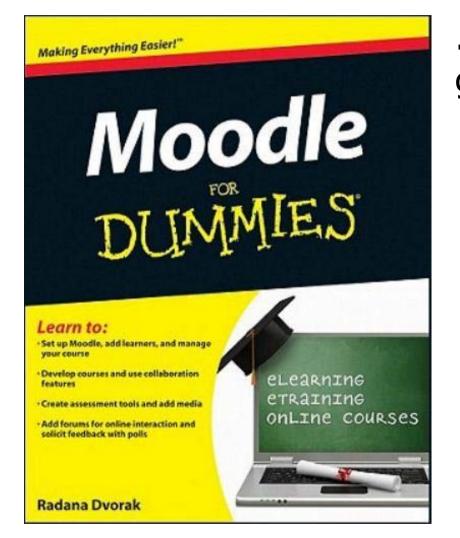
A Gamble? An Uphill Struggle?



CAS Handheld of Choice

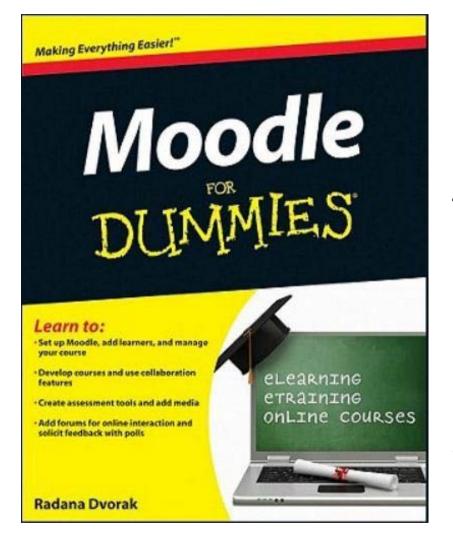


Generation Z (born 1995–2015)



... The learners of this generation are

Generation Z (born 1995–2015)



... The learners of this generation are impatient, seem to expect immediate results, and multitask with tech devices at exceptional speeds. They don't like to read instructions — most jump in and get on with it. Their expectations of technology are demanding. This generation will take to eLearning and will push boundaries.

Generation Z's Compatibility with CAS

- ✓ Are play-oriented.
- ✓ Expect immediate results.
- ✓ Expect information to come to them or accessible at one click.
- ✓ Do not read instructions, especially step-by-step outlines, but jump straight in.
- ✓ Do not process as linearly as previous generations.
- ✓ Are impatient if technology is not quick enough — they find something else to do.
- \checkmark Trust the medium.

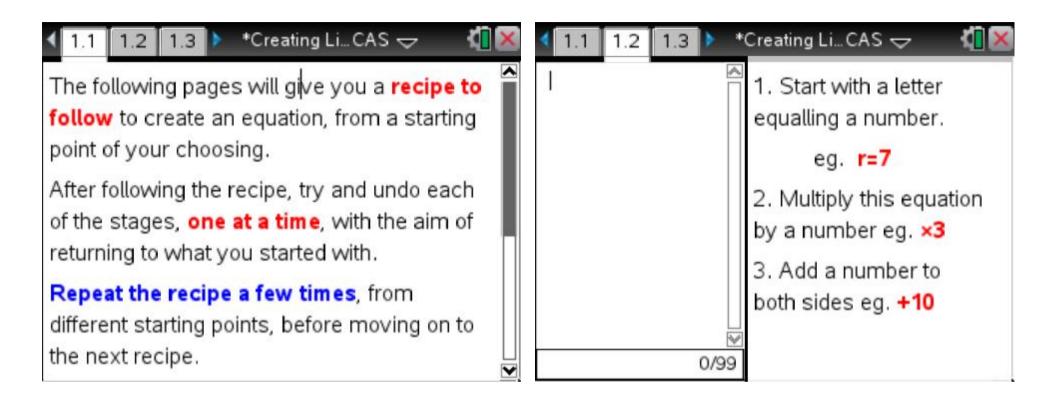
Generation Z's Compatibility with CAS

- ✓ Are play-oriented.
- ✓ Expect immediate results.
- ✓ Expect information to come to them or accessible at one click.
- ✓ Do not read instructions, especially step-by-step outlines, but jump straight in.
- ✓ Do not process as linearly as previous generations.
- ✓ Are impatient if technology is not quick enough — they find something else to do.
- \checkmark Trust the medium.

- Look at graphics first and access text-based media last.
- Process things at "twitch speed" (ie "more than 100 images a minute.")
- Do not stay with tasks as long.
- Do not expect things to go wrong.



Creating Linear Equations



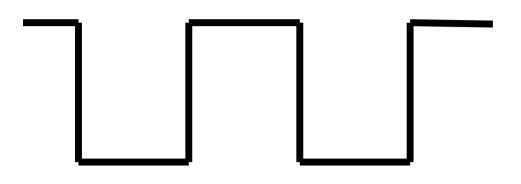
randomequation()

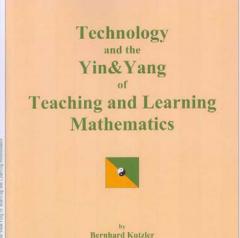
 $ax \pm b = \pm d$ $Ax \pm b = ax \pm d$ $ax \pm b = Ax \pm d$ $ax \pm b = cx \pm d$ $ax \pm b = d - cx$ $b - ax = cx \pm d$ b - ax = d - cx

Simultanous Linear Equations

1.1 1.2 1.3 Sim Equat	ioCAS 🗢 🛛 🚺	X		
© This page shows an example of its use				
$x+2 \cdot y=12$	$x+2 \cdot y=12$			
$3 \cdot x - 4 \cdot y = 15$	$3 \cdot x - 4 \cdot y = 15$			
$multiplyby2(x+2\cdot y=12)$	$2 \cdot x + 4 \cdot y = 24$			
$add(3 \cdot x - 4 \cdot y = 15, 2 \cdot x + 4 \cdot y)$	v=24) 5 x=39			
© and then solve this as normal.				
[]]				

Avoiding Interruptions





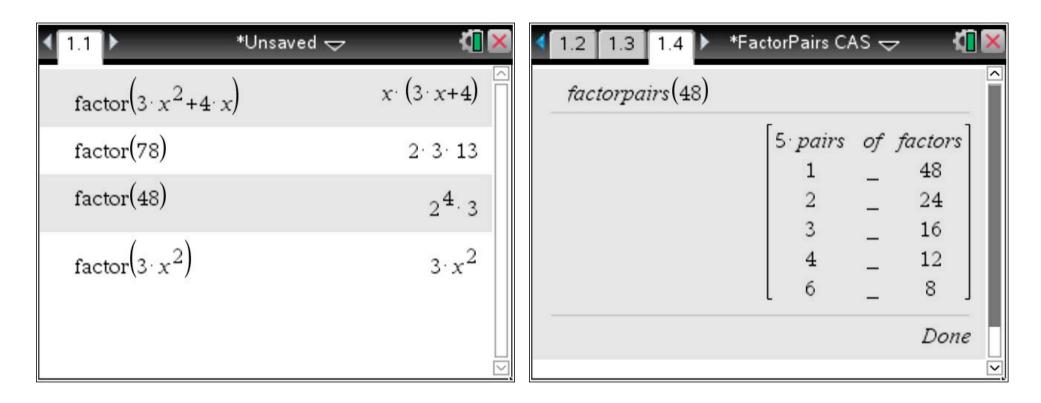
BK-01

"The picture demonstrates that a student, while trying to learn a new skill, repeatedly has to interrupt the learning process in order to perform a simplification"

Factor Pairs

The Issue

More Helpful

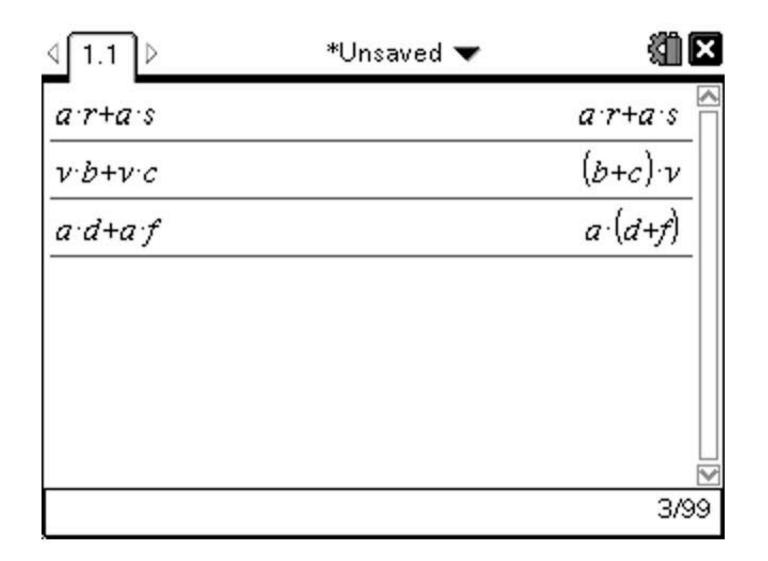


Beneficial when preparing for Factorising expressions

Unexpected Behaviour – 1

√ 1.1 ▷	*Unsaved 🔻	A 10
a·r+a·s		a·r+a·s
v·b+v·c		$(b+c)\cdot\nu$
1		
		2/99

Unexpected Behaviour – 2



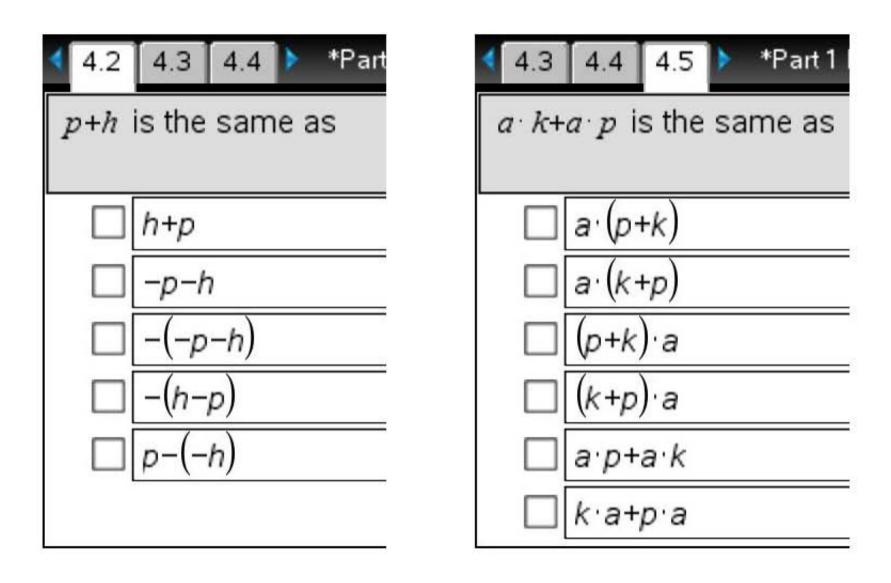
Rearranging Equations

What do **we** think about when faced with rearranging these formula to make x the subject....

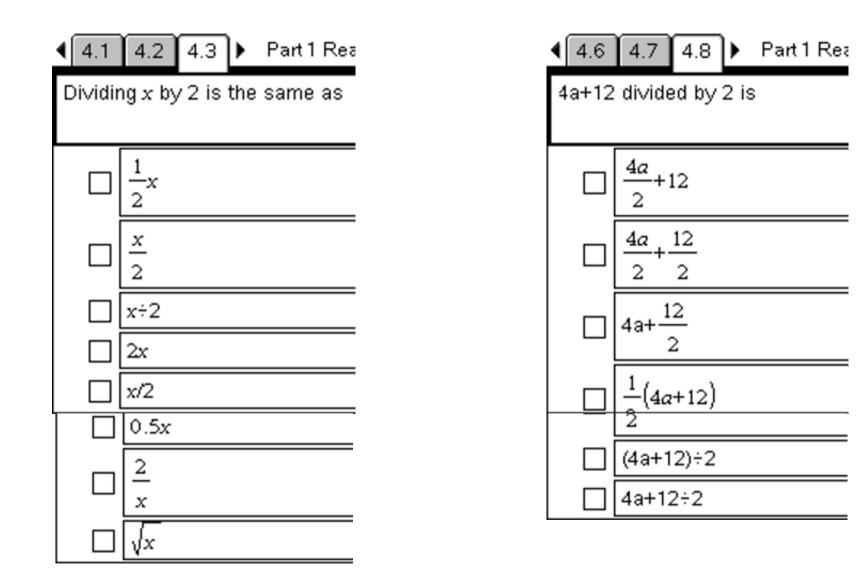
$$kx + m = n \qquad \qquad \frac{a}{x} + b = c \qquad \qquad r = \frac{x + p}{x - p}$$

I **now** know why students find rearranging so tricky!

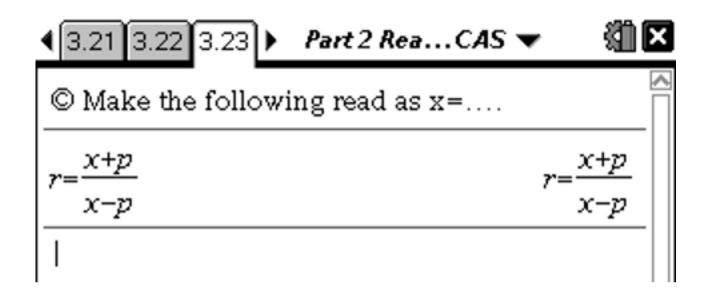
Preparing to use CAS



Preparing to use CAS

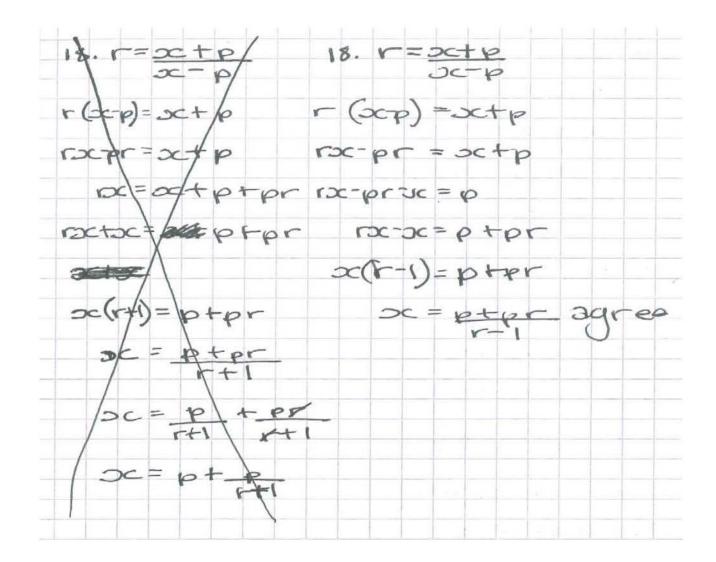


Rearranging Formulae



Video of Elizabeth solving this.

Elizabeth's Jotter



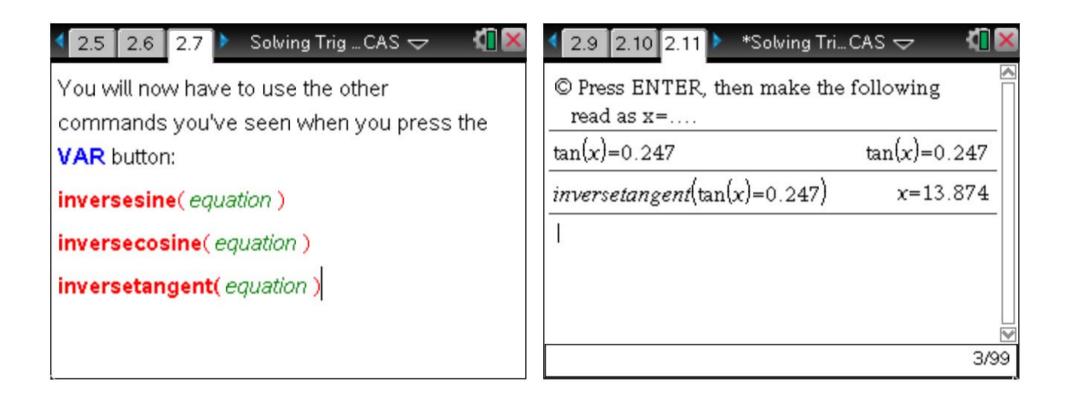
Elizabeth's Test Homework (2 weeks later)

14 - R = rsR(rts)=rs RitsREG SREFS-RR -rst SR=-Rr s(R-r) = - Rr

More....



Trigonometric Equations

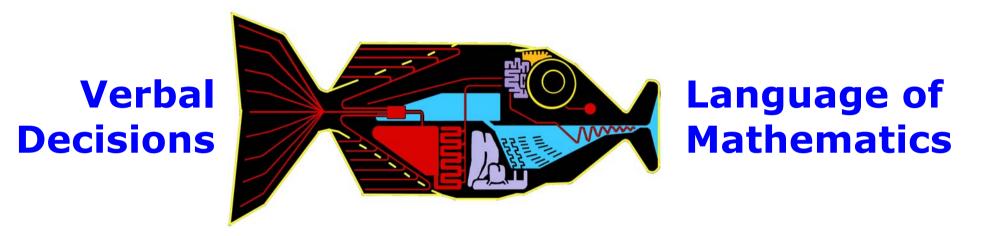


Further ... Quicker

Feedback Messages

2.20 2.21 2.22 *Solvir	ng Tri CAS 🤝 🛛 🐔 🔀	
© Press ENTER, then mak read as x=	e the following	
$5 \cdot \sin(x) - 4 = 0$.	$5 \cdot \sin(x) - 4 = 0$.	
$(5 \cdot \sin(x) - 4 = 0) + 4$	$5 \cdot \sin(x) = 4.$	
$inversesine(5 \cdot \sin(x) = 4.)$		
"Inverse sine not appropriate"		
	4/99	

Babel Fish*



* Hitchhiker's Guide to the Galaxy, Douglas Adams, 1981

Problem solving by reasoning

Problem solving by reasoning

Modelling Operating Interpreting Reasoning

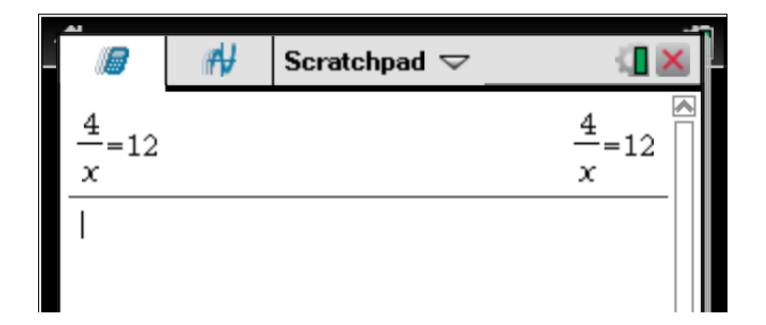
Problem solving by reasoning

Modelling Operating Interpreting Reasoning

Doing → **Planning**

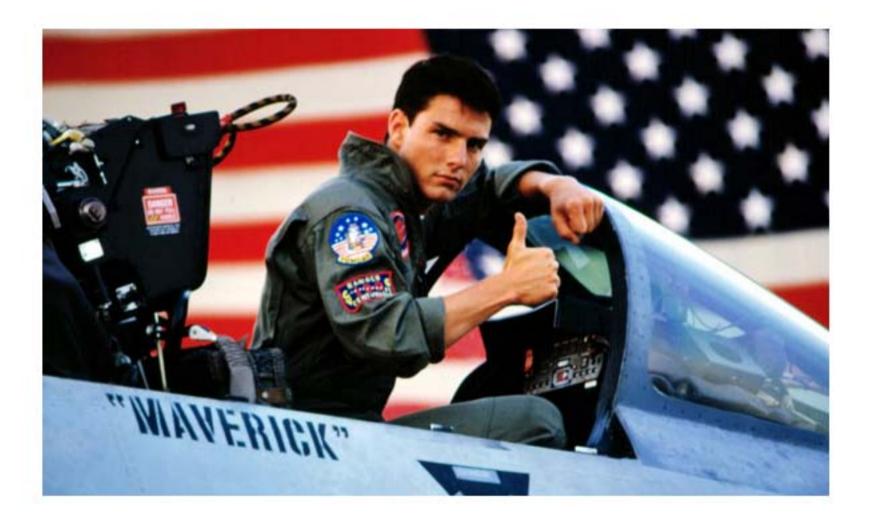
The Sine Rule

$$\frac{a}{\sin(A)} = \frac{b}{\sin(B)} \qquad or \qquad \frac{\sin(A)}{a} = \frac{\sin(B)}{b}$$

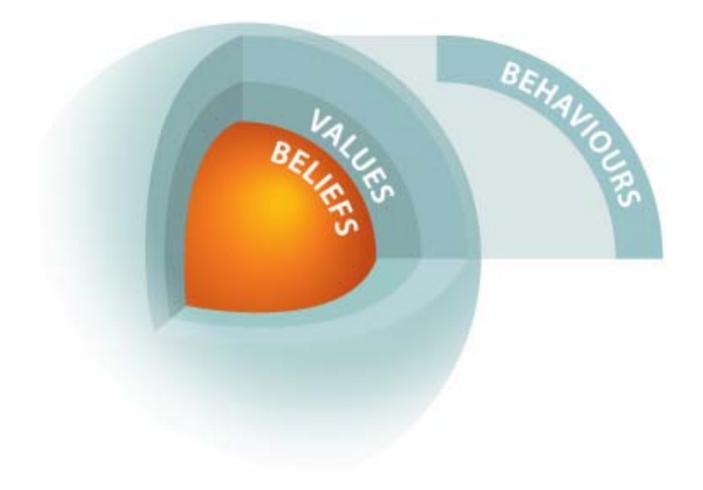


`The Lesson that Crashed'

Why do I use CAS?



Why would you use CAS?



CAS vs Established Approaches

Are traditional approaches as successful as you think?

CAS vs Established Approaches

Are traditional approaches as successful as you think?

Or are they mainly successful on specially designed tasks?

CAS vs Established Approaches

Are traditional approaches as successful as you think?

Or are they mainly successful on specially designed tasks?

Do established methods deserve their exalted status?

Curious Questions?



Want Copies of Everything? www.CalculatorSoftware.co.uk/nspire

Thank you for your attention. Have a great Symposium!

Nevil Hopley

T³ National Trainer, Scotland & UK.

Head of Mathematics Department George Watson's College, Edinburgh

CAS User